

Bellwork: 5/22/13

Solve each equation:

1) $\log_2(2x+16) = 3$

$$\begin{aligned} 2^3 &= 2x+16 \\ 8 &= 2x+16 \\ -16 &\quad -16 \\ \hline -8 &= 2x \\ x &= -4 \end{aligned}$$

2) $\log_5(x^2-7x) = \log_5 30$

$$\begin{aligned} x^2-7x &= 30 \\ x^2-7x-30 &= 0 \\ (x-10)(x+3) &= 0 \\ x &= 10, -3 \end{aligned}$$

Type 3: LOG + LOG = # - condense to one log, swirl and solve.

10) $\log_3 8 + \log_3 6x = 5$

$$\begin{aligned} \log_3 8 \cdot 6x &= 5 \\ \log_3 48x &= 5 \\ 3^5 &= 48x \\ \frac{243}{48} &= \frac{48x}{48} \\ \frac{81}{16} &= x \end{aligned}$$

Try these:

13) $\log x + \log 5 = 2$

$$\begin{aligned} \log_{10} 5x &= 2 \\ 10^2 &= 5x \\ 100 &= 5x \\ x &= 20 \end{aligned}$$

11) $\log_5(2x+1) + \log_5 3 = 8$

$$\begin{aligned} \log x(x+21) &= 2 \\ \log_{10} x^2 + 21x &= 2 \\ 10^2 &= x^2 + 21x \\ 100 &= x^2 + 21x \\ x^2 + 21x - 100 &= 0 \\ (x+25)(x-4) &= 0 \\ x &= -25, 4 \end{aligned}$$

log 0 can't happen

$x=4$

14) $\log_4 25 + \log_4 x^2 = 1$

$$\begin{aligned} \log_4 \frac{25}{x^2} &= 1 \\ x^2 \cdot 4^1 &= \frac{25}{x^2} \cdot x^2 \\ 4x^2 &= 25 \\ 4x^2 - 25 &= 0 \\ (2x+5)(2x-5) &= 0 \\ x &= -\frac{5}{2}, \frac{5}{2} \end{aligned}$$

works!

Type 4: $\text{LOG} + \text{LOG} = \text{LOG}$ - condense two logs to one, then cancel and solve.

15) $\log_5 x \oplus \log_5 6 = \log_5 16$

$$\log_5 \frac{x}{6} = \log_5 16$$

$$\frac{x}{6} = 16$$

$$\boxed{x = 96}$$

Try these:

17) $\log_4 x - \log_4 3 = \log_4 24$

16) $\log(x+1) \oplus \log x = \log 12$

$$\log (x+1)x = \log 12$$

$$x^2 + 1x = 12$$

$$x^2 + x - 12 = 0$$

$$(x+4)(x-3)$$

$$x = 3, -4$$

$$\boxed{x = 3}$$

18) $\log(x-3) \oplus \log x = \log 4$

$$\log x(x-3) = \log 4$$

$$x^2 - 3x = 4$$

$$x^2 - 3x - 4 = 0$$

$$(x-4)(x+1) \quad x = 4, -1$$

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18) $\log x \oplus \log 7 = \log 37$

$$\log 7x = \log 37$$

$$7x = 37$$

$$\boxed{x = \frac{37}{7}}$$

$$\textcircled{19} \log_8 2 \oplus \log_8 4x^2 = 1$$

$$\log_8 2 \cdot 4x^2 = 1$$

$$\log_8 8x^2 = 1$$

$$8^1 = 8x^2$$

$$8 = 8x^2$$

$$8x^2 - 8 = 0$$

$$8(x^2 - 1) = 0$$

$$(x-1)(x+1) = 0$$

$$x = 1, -1$$

$$\textcircled{20} \log_9 (x+6) \ominus \log_9 x = \log_9 2$$

$$\cancel{\log_9} \frac{x+6}{x} = \cancel{\log_9} 2$$

$$\frac{x+6}{x} = 2$$

$$\begin{array}{r} x+6 = 2x \\ -x \quad -x \\ \hline 6 = x \end{array}$$

$$\textcircled{21} \log_6 (x+1) \ominus \log_6 x = \log_6 29$$

$$\cancel{\log_6} \frac{x+1}{x} = \cancel{\log_6} 29$$

$$\cancel{x} \cdot \frac{x+1}{\cancel{x}} = \frac{29x}{1}$$

$$x = \frac{1}{28}$$

$$\begin{array}{r} 29x = x+1 \\ -x \quad -x \\ \hline \end{array}$$

$$\frac{28x}{28} = \frac{1}{28}$$

$$\textcircled{22} \log_5 6 \overset{*}{+} \log_5 2x^2 = \log_5 48$$

$$\log_5 6 \cdot 2x^2 = \log_5 48$$

$$\cancel{\log_5} 12x^2 = \cancel{\log_5} 48$$

$$12x^2 = 48$$

$$12x^2 - 48 = 0$$

$$12(x^2 - 4) = 0$$

$$(x-2)(x+2) = 0$$

$$x = 2, -2$$

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